

(Time: 3 hours)

Max. Marks: 80

N.B. (1) Question No. 1 is compulsory.**(2) Answer any three questions from Q.2 to Q.6.****(3) Use of Statistical Tables permitted.****(4) Figures to the right indicate full marks.**

Q1 a) If $A = \begin{bmatrix} 2 & 4 \\ 0 & 3 \end{bmatrix}$ then find the Eigen values of $A^3 + 6A^{-1} + 2I$ [5]

b) Evaluate $\int_0^{1+i} (x^2 + iy) dz$, along the path (i) $y = x$, (ii) $y = x^2$ [5]

c) Write the dual of the following problem [5]

$$\text{Maximise } z = 3x_1 + 10x_2 + 2x_3$$

$$\text{subject to } 2x_1 + 3x_2 + 2x_3 \leq 8$$

$$3x_1 - 2x_2 + 4x_3 = 4$$

$$x_1, x_2, x_3 \geq 0$$

d) A certain drug administered to 12 patients resulted in the following change in their Blood Pressure

5, 2, 8, -1, 3, 0, 6, -2, 1, 5, 0, 4 [5]

Can we conclude that drug increase the Blood Pressure?

Q2 (a) Using Cauchy's residue theorem evaluate [6]

$$\int_c \frac{1-2z}{z(z-1)(z-2)} dz, \text{ Where } c \text{ is } |z|=1.5$$

(b) Verify Cayley-Hamilton theorem and find A^{-1} for $A = \begin{bmatrix} 1 & 8 \\ 2 & 1 \end{bmatrix}$. Hence, find $2A^3 - A^2 - 35A - 44I$. [6]

(c) Solve by Simplex Method [8]

$$\text{Maximise } z = 4x_1 + 10x_2$$

$$\text{Subject to } 2x_1 + x_2 \leq 50$$

$$2x_1 + 5x_2 \leq 100$$

$$2x_1 + 3x_2 \leq 90$$

$$x_1, x_2 \geq 0$$

Q3 a) Based on the following data determine if there is a relation between literacy and smoking

	Smokers	Non-smokers	[6]
Literates	83	57	
Illiterates	45	68	

(Given that Critical value of chi-square 1 d. f and 5% L.O.S is 3.841

b) Obtain Laurent's series expansion of $f(z) = \frac{1}{z^2+4z+3}$ [6]

when (i) $|z| < 1$ (ii) $1 < |z| < 3$ (iii) $|z| > 3$

c) Using the method of Lagrangian multipliers solve the following N.L.P.P [8]

Optimise $z = x_1^2 + x_2^2 + x_3^2$

Subject to $x_1 + x_2 + 3x_3 = 2$

$$5x_1 + 2x_2 + x_3 = 5$$

$$x_1, x_2, x_3 \geq 0$$

Q4a) Using the method of Lagrange's multipliers solve the following N.L.P.P [6]

Optimise $z = x_1^2 + x_2^2 + x_3^2 - 10x_1 - 6x_2 - 4x_3$

Subject to $x_1 + x_2 + x_3 = 7$

$$x_1, x_2, x_3 \geq 0$$

b) Find the inverse Z-transform of $\frac{1}{z^2-3z+2}$, if ROC is (i) $|z| < 1$ (ii) $|z| > 2$ [6]

c) Show that the matrix $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ is diagonalizable. Find the transforming matrix and the diagonal matrix. [8]

Q5a) Find $Z\{f(k) * g(k)\}$ if $f(k) = \left(\frac{1}{2}\right)^k$, $g(k) = \cos\pi k$ [6]

b) Find the Eigen values and Eigen Vectors of the following matrix. [6]

$$A = \begin{bmatrix} 4 & 6 & 6 \\ 1 & 3 & 2 \\ -1 & -5 & -2 \end{bmatrix}$$

c) Solve by the dual Simplex Method

[8]

$$\text{Minimise } z = x_1 + x_2$$

$$\text{Subject to } 2x_1 + x_2 \geq 2$$

$$-x_1 - x_2 \geq 1$$

$$x_1, x_2 \geq 0$$

Q6a) Find $Z\{2^k \cos(3k + 2)\}, k \geq 0$.

[6]

b) If the heights of 500 students is normally distributed with mean 68 inches and standard deviation 4 inches, estimate the number of students having heights (i) greater than 72 inches

(ii) less than 62 inches (iii) between 65 and 71 inches

[6]

c) Using Kuhn Tucker conditions, solve the following NLPP

[8]

$$\text{Maximise } z = 2x_1^2 - 7x_2^2 + 12x_1x_2$$

$$\text{Subject to } 2x_1 + 5x_2 \leq 98$$

$$x_1, x_2 \geq 0$$

Duration: 3hrs

[Max Marks:80]

- N.B. : (1) Question No 1 is Compulsory.
(2) Attempt any three questions out of the remaining five.
(3) All questions carry equal marks.
(4) Assume suitable data, if required and state it clearly.

- 1 Attempt **any FOUR** **[20]**
- a Explain the Floating point Pipeline of Pentium Processor.
 - b What is the advantage of Memory Banking in 8086 Processor? Justify with example.
 - c Write an assembly language program for searching a Character in a Given String. (Consider your own String)
 - d Explain the following instructions: XLAT, DAA, LAHF, AAA related to 8086.
 - e Differentiate between real Mode, Virtual Mode and Protected Mode of 80386 Processor.
- 2 a Draw and explain write operation Timing diagram of 8086 Processor in Maximum mode. **[10]**
- b Draw and Explain the Master Slave Mode of 8259 Processor with Suitable example. Consider Slave 8259 connected to IR0 and IR4 of master. **[10]**
- 3 a Design 8086 microprocessor-based on following Specifications: **[10]**
- 1. MP 8086 working at 10MHz minimum mode.
 - 2. 64 KB ROM using 16KB Devices
 - 3. 32KB RAM using 16KB chips
- b Explain Mode 2 of 8255 with a neat block diagram. Show the CWR initialization. **[10]**
- 4 a Explain the 8257 DMA controller with the help of neat diagram and explain its Control Register Format. **[10]**
- b Write an ALP for 8086 to arrange 10 numbers in ascending order. **[10]**
- 5 a Explain the segment descriptor of 80386 processor. **[10]**
- b Explain the EFLAG REGISTER of 80386 Processor. **[10]**
- 6 a Explain the interrupt structure of 8086 processor. **[10]**
- b Explain the Branch Prediction Mechanism of Pentium Processor. **[10]**
